# Package: tsPI (via r-universe)

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**Title** Improved Prediction Intervals for ARIMA Processes and Structural Time Series

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Suggests testthat

Description Prediction intervals for ARIMA and structural time series models using importance sampling approach with uninformative priors for model parameters, leading to more accurate coverage probabilities in frequentist sense. Instead of sampling the future observations and hidden states of the state space representation of the model, only model parameters are sampled, and the method is based solving the equations corresponding to the conditional coverage probability of the prediction intervals. This makes method relatively fast compared to for example MCMC methods, and standard errors of prediction limits can also be computed straightforwardly.

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acv\_arma

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Compute a theoretical autocovariance function of ARMA process

# **Description**

Function acv\_arma computes a theoretical autocovariance function of ARMA process.

## Usage

```
acv_arma(phi, theta, n)
```

# Arguments

phi vector containing the AR parameters
theta vector containing the MA parameters
n length of the time series

## Value

vector of length n containing the autocovariances

# See Also

```
dacv_arma.
```

# Examples

```
## Example from Brockwell & Davis (1991, page 92-94) ## also in help page of ARMAacf (from stats) n \leftarrow 0:9 answer \leftarrow 2^{(-n)} * (32/3 + 8 * n) / (32/3) acv \leftarrow acv_arma(c(1.0, -0.25), 1.0, 10) all.equal(acv/acv[1], answer)
```

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arima_pi	Prediction Intervals for ARIMA Processes with Exogenous Variables
	Using Importance Sampling

# Description

Function arima\_pi computes prediction intervals for ARIMA processes with exogenous variables using importance sampling. For regression coefficients, diffuse (uninformative) prior is used, whereas multiple options for prior distributions for ARMA coefficients are supported.

# Usage

```
arima_pi(
 х,
 order,
 xreg = NULL,
 n_ahead = 1,
 level = 0.95,
 median = TRUE,
  se_limits = TRUE,
 prior = "uniform",
  custom_prior,
  custom_prior_args = NULL,
  nsim = 1000,
  invertibility = FALSE,
  last_only = FALSE,
  return_weights = FALSE,
)
```

## **Arguments**

x	vector containing the time series	
order	vector of length 3 with values p,d,q corresponding to the number of AR parameters, degree of differencing and number of MA parameters.	
xreg	matrix or data frame containing the exogenous variables (not including the intercept which is always included for non-differenced series)	
n_ahead	length of the forecast horizon.	
level	desired frequentist coverage probability of the prediction intervals.	
median	compute the median of the prediction interval.	
se_limits	compute the standard errors of the prediction interval limits.	
prior	prior to be used in importance sampling for AR and MA parameters. Defaults to uniform prior. Several Jeffreys' priors are also available (see jeffreys for details). If "custom", a user-defined custom prior is used (see next arguments). All priors assume that the ARMA parameters lie in stationarity/invertibility region.	

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#### Value

a list containing the prediction intervals. @references

- 1. Helske, J. and Nyblom, J. (2015). Improved frequentist prediction intervals for autoregressive models by simulation. In Siem Jan Koopman and Neil Shephard, editors, Unobserved Components and Time Series Econometrics. Oxford University Press. https://urn.fi/URN:NBN:fi:jyu-201603141839
- 2. Helske, J. and Nyblom, J. (2014). Improved frequentist prediction intervals for ARMA models by simulation. In Johan Knif and Bernd Pape, editors, Contributions to Mathematics, Statistics, Econometrics, and Finance: essays in honour of professor Seppo Pynnönen, number 296 in Acta Wasaensia, pages 71–86. University of Vaasa. https://urn.fi/URN:NBN:fi:jyu-201603141836

#### See Also

```
tsPI, struct_pi
```

#### **Examples**

```
set.seed(123)
x <- arima.sim(n = 30, model = list(ar = 0.9))

pred_arima <- predict(arima(x, order = c(1,0,0)), n.ahead = 10, se.fit = TRUE)
pred_arima <- cbind(pred = pred_arima$pred,
    lwr = pred_arima$pred - qnorm(0.975)*pred_arima$se,
    upr = pred_arima$pred + qnorm(0.975)*pred_arima$se)

pred <- arima_pi(x, order = c(1,0,0), n_ahead = 10)

ts.plot(ts.union(x,pred_arima, pred[,1:3]), col = c(1,2,2,2,3,3,3),
    lty = c(1,1,2,2,1,2,2))</pre>
```

avg\_coverage\_arima 5

avg_coverage_arima	Compute the average coverage of the prediction intervals computed
	by naive plug-in method and arima_pi

# Description

Computes expected coverage probabilities of the prediction intervals of ARMA process by simulating time series from the known model.

# Usage

```
avg_coverage_arima(
  phi = NULL,
  theta = NULL,
  d = 0,
  n,
  n_ahead = 1,
  nsim2,
  nsim = 100,
  level = 0.95,
  prior = "uniform",
  return_all_coverages = FALSE,
  ...
)
```

# Arguments

phi	vector containing the AR parameters			
theta	vector containing the MA parameters			
d	degree of differencing			
n	length of the time series			
n_ahead	length of the forecast horizon			
nsim2	number of simulations used in computing the expected coverage			
nsim	number of simulations used in importance sampling			
level	desired coverage probability of the prediction intervals			
prior	prior to be used in importance sampling. Multiple choices are allowed.			
return_all_coverages				
	return raw results i.e. coverages for each simulations. When FALSE (default), summary statistics are returned.			
	additional arguments to arima_pi.			

# Value

a list containing the coverage probabilities

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### See Also

```
arima_pi.
```

### **Examples**

```
## Not run:
set.seed(123)
# takes a while, notice se, increase nsim2 to get more accurate results
avg_coverage_arima(phi = 0.9, n = 50, n_ahead = 10, nsim2 = 100)
avg_coverage_arima(phi = 0.9, theta = -0.6, n = 50, n_ahead = 10, nsim2 = 100)
## End(Not run)
```

avg\_coverage\_struct

Compute the average coverage of the prediction intervals computed by struct\_pi and plug-in method

#### **Description**

Computes expected coverage probabilities of the prediction intervals of structural time series model. Note that for the plug-in method only standard deviations are assumed to be identical to their estimates, but the initial values for the states are still treated as diffuse. Because of this, plug-in method often performs relatively well in case of structural time series models compared to similar type of ARIMA models (local level and local linear trend models are closely related to ARIMA(0,1,1) and ARIMA(0,2,2) models), and in some cases even outperforms the importance sampling approach with uniform prior (see examples). This is not suprising, as local level and local linear trend models are closely related to ARIMA(0,1,1) and ARIMA(0,2,2) models, and the effect of uncertainty in MA components is not as significant as the uncertainty of AR components

#### **Usage**

```
avg_coverage_struct(
  type = c("level", "trend", "BSM"),
  sds,
  frequency = 1,
  n,
  n_ahead = 1,
  nsim2,
  nsim = 100,
  level = 0.95,
  prior = "uniform",
  return_all_coverages = FALSE,
  ...
)
```

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#### **Arguments**

Type of model. See struct\_pi. type sds vector containing the standard deviations of the model (observation error, level, slope, and seasonal). frequency frequency of the series, needed for seasonal component. length of the time series n\_ahead length of the forecast horizon nsim2 number of simulations used in computing the expected coverage number of simulations used in importance sampling nsim level desired coverage probability of the prediction intervals prior prior to be used in importance sampling. return\_all\_coverages return raw results i.e. coverages for each simulations. When FALSE (default), summary statistics are returned. additional arguments to struct\_pi.

## Value

a list containing the coverage probabilities

#### See Also

```
struct_pi.
```

# **Examples**

```
## Not run:
set.seed(123)
# takes a while, notice se, increase nsim2 to get more accurate results
avg_coverage_struct(type = "level", sds = c(1, 0.1), n = 50, n_ahead = 10, nsim2 = 100)
avg_coverage_struct(type = "BSM", sds = c(1, 1, 0.1, 10),
    frequency = 4, n = 50, n_ahead = 10, nsim2 = 100)
## End(Not run)
```

dacv\_arma

Compute the partial derivatives of theoretical autocovariance function of ARMA process

## **Description**

Function dacv\_arma computes the partial derivatives of theoretical autocovariance function of ARMA process

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#### Usage

```
dacv_arma(phi, theta, n)
```

#### **Arguments**

phi vector containing the AR parameters theta vector containing the MA parameters

n length of the time series

#### Value

matrix containing the partial derivatives autocovariances, each column corresponding to one parameter of vector (phi,theta) (in that order)

#### See Also

acv\_arma.

information\_arma

Large Sample Approximation of Information Matrix for ARMA process

## Description

Fortran implementation of InformationMatrixARMA function of FitARMA package, except that the function uses the same ARMA model definition as arima, where both the AR and MA parts of the model are on the right side of the equation, i.e. MA coefficients differ in sign compared to InformationMatrixARMA.

#### Usage

```
information_arma(phi = NULL, theta = NULL)
```

## **Arguments**

phi Autoregressive coefficients. theta Moving average coefficients.

#### Value

Large sample approximation of information matrix for ARMA process.

#### References

- 1. Box, G. and Jenkins, G. (1970). Time Series Analysis: Forecasting and Control. San Francisco: Holden-Day.
- 2. McLeod, A. I. and Zhang, Y., (2007). Faster ARMA maximum likelihood estimation Computational Statistics & Data Analysis 52(4) URL https://dx.doi.org/10.1016/j.csda.2007.07.020

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jeffreys	Compute of prior	different	types	of	importance	weights	based o	n Jeffi	reys's	

# Description

These functions compute different types of importance weights based on Jeffreys's priors used in arima\_pi.

# Usage

```
approx_joint_jeffreys(psi, xreg = NULL, p, q, n)
approx_marginal_jeffreys(psi, p, q)
exact_joint_jeffreys(psi, xreg = NULL, p, q, n)
exact_marginal_jeffreys(psi, p, q, n)
```

## **Arguments**

ps1	vector containing the ar and ma parameters (in that order).
xreg	matrix or data frame containing the exogenous variables (not including the intercept which is always included for non-differenced series)
р	number of ar parameters
q	number of ma parameters
n	length of the time series

# See Also

```
arima_pi.
```

struct_pi	Prediction Intervals for Structural Time Series with Exogenous Variables Using Importance Sampling
	antes osing importance sampling

# Description

Function struct\_pi computes prediction intervals for structural time series with exogenous variables using importance sampling.

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### Usage

```
struct_pi(
    x,
    type = c("level", "trend", "BSM"),
    xreg = NULL,
    n_ahead = 1,
    level = 0.95,
    median = TRUE,
    se_limits = TRUE,
    prior = "uniform",
    custom_prior,
    custom_prior_args = NULL,
    nsim = 1000,
    inits = NULL,
    last_only = FALSE,
    return_weights = FALSE
)
```

### **Arguments**

X	vector containing the time series
---	-----------------------------------

type of model. Possible options are "level", "trend" and "BSM", correspond-

ing to local level, local linear trend, and local linear trend model with seasonal

component.

xreg matrix or data frame containing the exogenous variables (not including the in-

tercept which is always included for non-differenced series)

n\_ahead length of the forecast horizon.

level desired frequentist coverage probability of the prediction intervals.

median compute the median of the prediction interval.

se\_limits compute the standard errors of the prediction interval limits.

prior prior to be used in importance sampling for log-sd parameters. Defaults to uni-

form prior on logarithm of standard deviations (with constraints that all variances are smaller than 1e7). If "custom", a user-defined custom prior is used

(see next arguments).

custom\_prior function for computing custom prior. First argument must be a vector containing

the log-variance parameters (observation error, level, slope, and seasonal).

custom\_prior\_args

list containing additional arguments to custom\_prior.

nsim number of simulations used in importance sampling. Default is 1000.

inits initial values for log-sds

last\_only compute the prediction intervals only for the last prediction step.

return\_weights Return (scaled) weights used in importance sampling.

#### Value

a list containing the prediction intervals.

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#### See Also

```
tsPI, arima_pi @references
```

1. Helske, J. (2015). Prediction and interpolation of time series by state space models. University of Jyväskylä. PhD thesis, Report 152. https://urn.fi/URN:NBN:fi:jyu-201603111829

#### **Examples**

```
pred_StructTS <- predict(StructTS(Nile, type ="level"), n.ahead = 10, se.fit = TRUE)
pred_StructTS <- cbind(pred = pred_StructTS$pred,
    lwr = pred_StructTS$pred - qnorm(0.975)*pred_StructTS$se,
    upr = pred_StructTS$pred + qnorm(0.975)*pred_StructTS$se)

set.seed(123)
pred <- struct_pi(Nile, type = "level", n_ahead = 10)

ts.plot(ts.union(Nile,pred_StructTS, pred[,1:3]), col = c(1,2,2,2,3,3,3),
    lty = c(1,1,2,2,1,2,2))</pre>
```

tsPI

Improved Prediction Intervals for ARIMA Processes and Structural Time Series

## Description

Package tsPI computes prediction intervals for ARIMA and structural time series models by using importance sampling approach with uninformative priors for model parameters, leading to more accurate coverage probabilities in frequentist sense. Instead of sampling the future observations and hidden states of the state space representation of the model, only model parameters are sampled, and the method is based solving the equations corresponding to the conditional coverage probability of the prediction intervals. This makes method relatively fast compared to for example MCMC methods, and standard errors of prediction limits can also be computed straightforwardly.

#### References

- Helske, J. and Nyblom, J. (2013). Improved frequentist prediction intervals for autoregressive models by simulation. In Siem Jan Koopman and Neil Shephard, editors, Unobserved Components and Time Series Econometrics. Oxford University Press. In press.
- 2. Helske, J. and Nyblom, J. (2014). Improved frequentist prediction intervals for ARMA models by simulation. In Johan Knif and Bernd Pape, editors, Contributions to Mathematics, Statistics, Econometrics, and Finance: essays in honour of professor Seppo Pynnönen, number 296 in Acta Wasaensia, pages 71–86. University of Vaasa.
- 3. Helske, J. (2015). Prediction and interpolation of time series by state space models. University of Jyväskylä. PhD thesis, Report 152.

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